



DPP-2969

First Year B. Sc. (Sem. II) Examination

March/April - 2016

Paper - MCS 202 : Mathematics for Computer Science
(Theory of Matrices)

Time : Hours]

[Total Marks : 70

Instructions :

(1)

नीचे दशांशके निशानीवाणी विगतो उत्तरवडी पर अवश्य लपवी.
Fillup strictly the details of signs on your answer book.

Name of the Examination :

Name of the Subject :

Subject Code No. : Section No. (1, 2,.....):

Seat No. :

Student's Signature

- (2) All questions are compulsory.
- (3) Figures to the right indicate full marks.

Q:1 Answer the following Questions any five: [10]

1. Define equal matrices with illustration.
2. If $A = \begin{bmatrix} 0 & i \\ -i & 0 \end{bmatrix}$ and $C = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$ then show that $A^2 = B^2$
3. Define Transpose of matrix with illustration.
4. Find A^{-1} for the matrix $A = \begin{bmatrix} 2 & 1 \\ 3 & 0 \end{bmatrix}$
5. Prove that if A and B are non-singular matrices then $A^{-1}B$ and BA^{-1} are similar matrices.
6. If $A = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix}$ then find A^{-1}
7. When does a non-homogeneous system of equations have infinite solution?

Q: 2 (A) For any square matrix A , prove that [05]

(i) $A + A^\theta$ is Hermitian.

(ii) $A - A^\theta$ is Skew Hermitian.

OR

Q: 2 (A) if A and B are $m \times n$ and $AB = BA$ matrices respectively then prove that $(AB)^T = B^T A^T$ [05]

Q: 2 (B) Attempt Any two [10]

(1) Prove that any square matrix A can be uniquely expressed as $P + iQ$

where both P and Q are Hermitian matrices.

(2) If $A = \begin{bmatrix} 1 & 3 \\ 0 & 2 \\ -1 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 3 & -4 \\ 2 & 0 & -2 & 1 \end{bmatrix}$ then find $A \bullet B$ also find $B \bullet A$ if possible.

(3) If $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$, $B = \begin{bmatrix} 3 & 1 \\ 4 & 2 \end{bmatrix}$ and $C = \begin{bmatrix} 5 & 1 \\ 7 & 4 \end{bmatrix}$ then show that

(i) $A(B+C) = AB+AC$ (ii) $(A+B)C = AC+BC$

(4) If $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$ then find the value of $A^2 - 4A - 5I$

Q: 3 (A) Define a non-singular matrix. Find the inverse of a matrix $A = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix}$ by applying

Elementary row operations. [05]

OR

Q: 3 (A) Verify that $(A \cdot B)^T = B^T \cdot A^T$ for the following matrices [05]

$A = \begin{bmatrix} 2 & 5 & 7 \\ 2 & -1 & 0 \\ 3 & 4 & 8 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 4 & 9 \\ 3 & -2 & 4 \\ 5 & 6 & 8 \end{bmatrix}$

Q: 3 (B) Attempt any two: [10]

(1) Prove that A is Hermitian if and only if $A^\theta = A$.

(2) If $A = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} a & b \\ 3 & 5 \end{bmatrix}$ then find the values of a and b if $AB = BA$

(3) Find the inverse of a matrix $A = \begin{bmatrix} 2 & 4 & 5 \\ 1 & 3 & 1 \\ 1 & 0 & 7 \end{bmatrix}$ by applying Elementary row operations.

(4) If $A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$, $\vec{B} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$ and $A \cdot B = \begin{bmatrix} 6 \\ 3 \\ 1 \end{bmatrix}$

Q:4 (A) Express the matrix $A = \begin{bmatrix} 0 & 1 & 3 & -1 & 3 & 1 \\ 0 & 1 & 3 & 0 & 2 & 3 \\ 0 & 2 & 6 & 1 & 3 & 9 \\ 0 & 4 & 12 & -2 & 10 & 7 \end{bmatrix}$ in the row reduced Echelon form [05]

OR

Q:4 (A) Find rank of the matrix $A = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 2 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ [05]

Q: 4(B) Attempt Any two [10]

(1) Find rank of the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 4 & 10 & 18 \end{bmatrix}$

(2) Find the inverse of a matrix $A = \begin{bmatrix} 2 & -1 & 4 \\ -3 & 0 & 1 \\ -1 & 1 & 2 \end{bmatrix}$ by applying Elementary row operations.

(3) Find rank of the matrix $A = \begin{bmatrix} 1 & 2 & 1 & 2 \\ 3 & 2 & 3 & 2 \\ -1 & -3 & 0 & 4 \\ 0 & 4 & -1 & -3 \end{bmatrix}$

(4) Express the matrix $A = \begin{bmatrix} 1 & -2 & 1 & 0 \\ -2 & 4 & 1 & 3 \\ 0 & 0 & 1 & 1 \\ 3 & -6 & 2 & -1 \end{bmatrix}$ in the row reduced Echelon form

Q:5(A) For what values of λ and μ , given non-homogeneous system of equations has [05]

(1) no solution (2) unique solution?

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 2 & \lambda \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 6 \\ 10 \\ \mu \end{bmatrix}$$

OR

Q: 5(A) Prove that the following system of equations has many solutions and solve it. [05]

$$\begin{aligned}3X + Y + Z &= 2 \\ X - 3Y + 2Z &= 1 \\ 7X - Y + 4Z &= 5\end{aligned}$$

Q: 5(B) Solve Any TWO of the following system of equations: [10]

(1)
$$\begin{aligned}X + 2Y + 3Z &= 0 \\ 3X + 4Y + 4Z &= 0 \\ 7X - 10Y + 12Z &= 0\end{aligned}$$

(3)
$$\begin{aligned}X + Y + 3Z &= 0 \\ X - Y + Z &= 0 \\ X - 2Y &= 0\end{aligned}$$

(2)
$$\begin{aligned}X + 2Y - Z &= 3 \\ 3X - Y + 4Z &= 1 \\ 2X - 2Y + 3Z &= 4 \\ X - Y + Z &= -1\end{aligned}$$

(4)
$$\begin{aligned}X + Y + Z &= 9 \\ 2X + 5Y + 7Z &= 52 \\ 2X + Y - Z &= 0\end{aligned}$$
